RNAiFold2T: Constraint Programming design of thermo-IRES switches

Juan Antonio Garcia-Martin,1 Ivan Dotu,2 Javier Fernandez-Chamorro,3 Gloria Lozano,3 Jorge Ramajo,3 Encarnacion Martinez-Salas3 and Peter Clote1,*

1Biology Department, Boston College, Chestnut Hill, MA 02467, USA, 2Department of Experimental and Health Sciences, Research Programme on Biomedical Informatics (GRIB), Universitat Pompeu Fabra. Dr. Aiguader 88, Barcelona, Spain and 3Centro de Biologia Molecular Severo Ochoa, Consejo Superior de Investigaciones Cientificas—Universidad Autonoma de Madrid, 28049 Madrid, Spain

*To whom correspondence should be addressed.

Abstract

**Motivation:** RNA thermometers (RNATs) are cis-regulatory elements that change secondary structure upon temperature shift. Often involved in the regulation of heat shock, cold shock and virulence genes, RNATs constitute an interesting potential resource in synthetic biology, where engineered RNATs could prove to be useful tools in biosensors and conditional gene regulation.

**Results:** Solving the 2-temperature inverse folding problem is critical for RNAT engineering. Here we introduce RNAiFold2T, the first Constraint Programming (CP) and Large Neighborhood Search (LNS) algorithms to solve this problem. Benchmarking tests of RNAiFold2T against existent programs (adaptive walk and genetic algorithm) inverse folding show that our software generates two orders of magnitude more solutions, thus allowing ample exploration of the space of solutions. Subsequently, solutions can be prioritized by computing various measures, including probability of target structure in the ensemble, melting temperature, etc. Using this strategy, we rationally designed two thermosensor internal ribosome entry site (thermo-IRES) elements, whose normalized cap-independent translation efficiency is approximately 50% greater at 42°C than 30°C, when tested in reticulocyte lysates. Translation efficiency is lower than that of the wild-type IRES element, which on the other hand is fully resistant to temperature shift-up. This appears to be the first purely computational design of functional RNA thermoswitches, and certainly the first purely computational design of functional thermo-IRES elements.

**Availability:** RNAiFold2T is publicly available as part of the new release RNAiFold3.0 at https://github.com/clotelab/RNAiFold and http://bioinformatics.bc.edu/clotelab/RNAiFold, which latter has a web server as well. The software is written in C++ and uses OR-Tools CP search engine.

**Contact:** clote@bc.edu

**Supplementary information:** Supplementary data are available at *Bioinformatics* online.

RNA thermometers (RNATs), also known as thermosensors, are cis-regulatory elements that change secondary structure upon temperature shift. Examples include (i) repression of heat shock gene expression (ROSE) elements (Nocker et al., 2001), which control the expression of small heat shock genes, such as hspA in Bradyrhizobium japonicum and ibpA in Escherichia coli; (ii) FourU elements (Waldminghaus et al., 2007b), such as the virulence factor LeCF in Yersinia pestis; and (iii) Hsp17 thermosensor (Kortmann et al., 2011; Torok et al., 2001), which controls membrane integrity of the cyanobacterium Synechocystis sp. PCC6803 under stress conditions, critical for photosynthetic activity. Additional examples are described in Kortmann and Narberhaus (2012). ROSE elements and FourU elements operate as temperature-sensitive, reversible zippers, while the Listeria monocytogenes prfA thermosensor (Johansson et al., 2002), phage λ cII thermoswitch (Altuvia et al., 1989) and *E.coli* CspA cold shock thermometer (Bae et al., 2000) operate in a switch-like fashion. Here, the helix of a zipper melts gradually with increasing temperature, returning to the original structure when temperature is reduced, while a switch consists of two mutually exclusive structures determined by temperature.
Several bioinformatics search methods exist to identify and predict candidate RNA thermometers. In Waldminghaus et al. (2007a) the database RNA-SURIBA (Structures of Untranslated Regions In Bacteria) was created, using regular expressions, particular structural motifs were detected in the minimum free energy (MFE) structure, as determined by mfold (Zuker, 2003). In contrast, the RNAtips web server (Churkin et al., 2014) and the RNAtherm (Churkin et al., 2014) web server both rely on base pairing probabilities computed at different temperatures using RNAfold from the Vienna RNA Package (Lorenz et al., 2011).

For some time now, RNA thermosensors have been recognized as an attractive target for rational design (Waldminghaus et al., 2008; Wieland and Hartig, 2007). Indeed, within the broader context of synthetic biology, rationally designed thermometers could be used as a thermostatic tool to control expression by temperature regulation (i.e. on-demand protein translation), or as even as a multifunctional nanoscale devices to measure temperature in the context of hyperthermic treatment of cancer cells, imaging or drug delivery (Lee and Kotov, 2007).

In Neupert et al. (2008), synthetic (zipper) thermosensors were manually designed to sequester the Shine-Dalgarno sequence AAGGAG within a single stem-loop structure containing 4–9 base pairs, several of which contained 1–2 bulges of size 1. In Waldminghaus et al. (2008), synthetic (switch) thermosensors were computationally designed to switch between a single stem-loop structure that sequesters the Shine-Dalgarno sequence GGAGG, and two shorter stem-loop structures where the Shine-Dalgarno sequence is found in the apical loop of the second stem-loop. In particular, the 2-temperature inverse folding (adaptive walk) program SwitchDesign (Flamm et al., 2001) was used to obtain 300 candidate sequences; only two candidate sequences survived after the application of several computational filters including the computation of melting curves with RNAheat (Lorenz et al., 2011). Since neither of these sequence displayed any temperature-dependent control of a reporter gene (bgaB) fusion, the top candidate sequence was used as a template in two rounds of error-prone mutagenesis followed by selection, resulting in a successful thermosensor—see Figure 5 of Waldminghaus et al. (2008). In Ogawa (2011), a non-temperature-dependent riboswitch was manually designed, which promotes cap-independent translation in wheat germ cell lysate only upon binding of the ligand theophylline. In Wachsmuth et al. (2013), a synthetic theophylline riboswitch was designed by a computational pipeline including inverse folding and experimentally shown to perform transcriptional regulation in Escherichia coli Top10 cells. In Saraglidiadis et al. (2013), a thermozyme was created by fusing a Salmonella RNA thermometer (RNAT) to a hammerhead ribozyme, followed by in vitro screening—thus showing that naturally occurring hammerheads and RNATs appear to be modules that can be combined. In Hoynes-O’Connor et al. (2015) small, heat-repressible RNA thermosensors (zippers) were manually designed in E.coli, which at low temperature sequester a cleavage site for RNaseE, and at high temperatures unfold to allow mRNA degradation.

Despite these impressive results, Kortmann and Narberhaus (2012) state that: ‘RNAs have little, if any sequence conservation and are difficult to predict from genome sequences. … Therefore, the bioinformatic prediction and rational design of functional RNAs has remained a major challenge.’

In this article, we introduce the software RNAiFold2T, capable of solving the inverse folding problem for two or more temperatures, i.e. generating one or more RNA sequences whose MFE secondary structures at temperatures $T_1$ and $T_2$ (resp. $T_1, \ldots, T_n$) are user-specified target structures $S_1$ and $S_2$ (resp. $S_1, \ldots, S_m$), or which reports that no such solution exists. RNAiFold2T is unique in that it implements two different algorithms—Constraint Programming (CP) and Large Neighborhood Search (LNS). CP is an exact, non-heuristic method that uses an exhaustive yet efficient branch-and-prune process, and is the only currently available software capable of generating all solutions or determining that no solution exists (since there are possibly exponentially many solutions, a complete solution is feasible only for structures of modest size). LNS uses a local search heuristic, complemented with local calls of CP to explore solutions of substructures of the target structures. We use RNAiFold2T to rationally design two thermo-ires elements, whose normalized cap-independent translation efficiency is approximately 50% greater at 42°C than 30°C, when tested in reticulocyte lysates. We then benchmark RNAiFold2T with the only two other programs that solve the 2-temperature inverse folding problem: the adaptive walk SwitchDesign (SD) (Flamm et al., 2001) and the genetic algorithm Frnakenstein (FRNA) (Lynso et al., 2012). RNAiFold2T CP generates two orders of magnitude more solutions than either, when all programs are run for 24 h, while the number of distinct problem instances that can be solved by RNAiFold2T LNS within 30 (resp. 60) min for short (resp. long) target structures is roughly comparable for each program. Finally, by analyzing existent RNATs found in the Rfam 12.0 database (Nawrocki et al., 2014), we determine that naturally occurring RNATs appear not to be optimized for the cost function [Equation (7)] of Flamm et al. (2001)], and that both SD and FRNA appear to generate solutions whose cost function value is substantially lower than that of naturally occurring RNATs, in contrast to solutions returned by RNAiFold2T.

1 Methods

1.1 Biochemical methods

1.1.1. Thermo-ires activity assay

Thermo-ires constructs were created by replacement of wild-type nucleotides at positions 417–462 in domain 5 of the foot-and-mouth disease virus (FMDV) IRES element, whose secondary structure is depicted in Figure 1 of Fernandez et al. (2011) and Figure 2 of Lozano et al. (2014). Six computationally designed thermo-ires elements were selected for validation, along with a negative control and the wild-type FMDV IRES element as positive control. Specifically, synthetic oligonucleotides containing the designed sequence (46 nts) in either positive or negative orientation were annealed in Tris 50 mM, pH 7.5, NaCl 100 mM, MgCl$_2$ 10 mM, 15 min at 37°C and subsequently inserted into the HindIII and Xhol restriction sites of pBIC, which harbors the wild-type IRES, linearized with the same enzymes. Colonies that carried the correct insert were then selected, and prior to expression analysis, the nucleotide sequence of the entire length of each region under study was determined (Macrogen).

In vitro transcription was performed for 1 h at 37°C using T7 RNA polymerase, as described in Lozano et al. (2015). RNA was extracted with phenol–chloroform, ethanol precipitated and then re-suspended in TE. Using gel electrophoresis, the transcripts were checked for integrity. Equal amounts of the RNAs synthesized in vitro were translated in 70% rabbit reticulocyte lysate (RRL) (Promega) supplemented with $^{35}$S-methionine (10 μCi), as described in Pino and al. (2013). Each experiment was independently repeated in triplicate, using the wild-type RNA as a control in all assays. Luciferase (LUC) and chloramphenicol acetyl transferase (CAT) activities were measured for the bicistronic plasmid, as previously described (Fernandez-Chamorro et al., 2014). In particular,
and/or target structures or hy-

with the Turner99,
or Andronescu partial
energy model with dangle treatment (-d0,
structure at temperature
T

RNAiFold2T uses CP to determine those sequences, whose MFE
1.2 Computational methods

intensity of the LUC band, as well as the CAT band, produced by each transcript was determined in a densitometer, and normalized
against the intensity of LUC and CAT bands produced by the wild
type RNA, set at 100%. Values represent the mean 

Luciferase activity reflects the efficiency of IRES-dependent
translation, while CAT activity reflects the efficiency of 5

translation; thus the ratio LUC/CAT was determined at 30

Examples of CP search for target structures
Fig. 1. Examples of CP search for helices versus EHwDs and EHwDs decom-
position heuristic. (a) MFE structure check made for EH on the left, and EHwD
on the right. In each line, either a new base pair (2 positions) or a new nucleo-
tide (1 position) is instantiated, following the variable order heuristic. For sim-
plication, this example assumes that correct value assignments are made in
each instantiation step. (b) Tree decomposition for target structure S1 (resp.
S2) at temperature T1 (resp. T2), using target structures for the FourU element
CP000647.1/1773227-1773291. The table on the right presents the order of
helix exploration using overlap, and overlap, heuristics

1.2 Computational methods
RNAiFold2T uses CP to determine those sequences, whose MFE
structure at temperature T1 (resp. T2) is identical to a user-specified
target structure S1 (resp. S2). The target structures S1, S2 can also be
hybridization complexes of two RNAs, rather than single secondary
structures. CP performs a complete, exhaustive (branch and prune)
exploration of the search space and therefore, it can return all pos-
sible solutions of the thermoswitch design problem or prove that no
solution exists (given an unlimited amount of time). In addition to

Fig. 2. Example of CP search for target structures S1 (top) at temperature
30°C, and S2 (bottom) at temperature 10°C. Undetermined positions are as-
sign (red) in the following order: base pairs are instantiated in lines
1,2,3,4,5,13; unpaired positions in lines 6,7,8,9,10,14; a closing base pair in
line 11; a dangling position in line 12. When the left nucleotide of a base pair
is instantiated to C (resp. A), then propagation of the base pairing constraint
reduces the domain of possible values of the right nucleotide of the base pair
from {A,C,G,U} to the set {G} (resp. {U})—this happens in lines 1, 6–9. For
simplification, this example assumes that correct value assignments always
occur at each search step

CP, RNAiFold2T also supports LNS, a fast local (not complete)
search metaheuristic that employs CP to exhaustively explore large
neighborhoods of every candidate solution at each iteration step. Moreover,
since it is written in C++ using the OR-Tools engine
https://github.com/google/or-tools, together with plug-ins to Vienna
RNA Package (Lorenz et al., 2011) and RNAstructure (Reuter and
Mathews, 2010), the user can install and run RNAiFold2T locally,
thus permitting much longer execution times than supported by our
web server.

The overall methodology of RNAiFold2T is similar to its precur-
sor, RNAiFold 2.0 (Garcia-Martín et al., 2012, 2015); however,
as explained below, there are a number of algorithmic details that are
new and not present in RNAiFold 2.0—decomposition tree for 2 or
more target structures, novel constraints that are underlined below,
variable (helix) and value heuristics that are proper only to
RNAiFold2T, the introduction of two types of restart heuristic in
LNS to ensure a good trade-off between exploration of promising
regions of the search space versus the exploration of remote portions
of the search space. RNAiFold2T cleanly separates all constraints
from the CP or LNS solver, thus permitting our software to be ex-
tended to support any future desirable constraints. Current con-
straints supported by RNAiFold2T include the following (novel
constraints underlined): full and/or partial target structures or hy-
bridization complexes at two temperatures; a plug-in to determine
MFE structure using either RNAfold (Lorenz et al., 2011) or
RNAstructure (Reuter and Mathews, 2010) with the Turner99,
Turner2004 (Turner and Mathews, 2010) or Andronescu
(Andronescu et al., 2007) energy model with dangle treatment (-d0,
-d1, -d2, -d3 corresponding respectively to no dangle, max of 5’
and 3’ dangle, sum of 5’ and 3’ dangle, sum of 5’ and 3’ dangle with co-
axial stacking); IUPAC nucleotide constraints, IUPAC amino acid
constraints that require all returned RNA sequences to code speci-
fied peptides in one or more overlapping reading frames, structural
compatibility and structural incompatibility constraints, etc.
Additionally, RNAiFold2T can determine a user-specified number
of solutions, all solutions (given sufficient time), or whether no
solution exists. Indeed, memory requirements for RNAiFold2T are minimal, and since there are no memory leaks, the software can be run for weeks.

In developing a CP solution to a given problem the main tasks are to define the problem (specify variables, domains and constraints) and to define the search procedure. The extension of the model from RNAiFold2.0 is trivial and consists of adding new constraints for the helices corresponding to the second structure. The search procedure, however, must be adapted to the new difficulties imposed by the 2-temperature problem. New variable and value ordering heuristics are needed in order to solve 2-temperature inverse folding efficiently (Supplementary Tables S1 and S2). The algorithmic details related to the new search procedure are explained below:

1.3 Structure decomposition

As in other inverse folding methods, such as RNAinverse (Lorenz et al., 2011), NUPACK (Zadeh et al., 2011), etc., we rely on a decomposition tree of the structure into independent helices, called extended helices (EHs) and extended helices with dangles (EHwDs).

See Supplementary Material for definitions of EH, EHwD and decomposition tree, and see Figure 1 for an illustration of the EHwD decomposition tree for a FourU thermometer. Decomposition trees play a special role in RNAiFold2T for the following reasons: (i) each node in the decomposition tree is a constraint; (ii) the helix and variable heuristics (described later) cause the search tree to be searched in a specific order.

To improve efficiency in solving multi-temperature inverse folding, we investigated various helix and value heuristics, which steer the search within a search space defined by a composite decomposition tree, comprising subtrees for each target structure at the corresponding temperature. The helix and value heuristics are new and not part of RNAiFold 2.0.

Consider the 65 nt FourU RNA thermometer whose MFE structures determined by RNAfold from Vienna RNA Package 2.1.9 (Lorenz et al., 2011) at 37°C and 53°C are given in dot-bracket notation by

\[
\text{sequence taken from the 5'UTR of the Salmonella agsA gene. Giving labels as described to nodes in the EHwD decomposition trees } T_1, T_2 \text{ respectively for } S_1 \text{ and } S_2, \text{ we find the EHwD decomposition of } S_1 \text{ has EHwD 0 from positions 1 to 65, EHwD 1 from positions 1 to 19, and EHwD 2 from positions 23 to 58, while the EHwD decomposition of } S_2 \text{ has EHwD 4 from positions 1 to 65, EHwD 5 from positions 14 to 65, and EHwD 5 from positions 23 to 58. The lower portion of Figure 1 depicts the EHwD decomposition trees for temperatures } T_1, T_2, \text{ joined together with a (dummy) root that corresponds to the solution returned by RNAiFold2T.}

It can happen that the MFE structure of an EH does not agree with the target substructure, while that of the EH with dangles does. This is the reason that the EH decomposition trees of RNAiFold 1.0 (Garcia-Martin et al., 2012) were replaced by EHwD decomposition trees in RNAiFold 2.0 (Garcia-Martin et al., 2015), and why EHwD trees are used in RNAiFold2T.

In the CP and LNS search strategy, whenever a subsequence corresponding to a node of the decomposition tree has been instantiated, a check is made to determine whether the MFE structure of the subsequence is identical to the target substructure. In the case of structural disagreement, the instantiated subsequence is discarded and backtracking occurs.

For any solution sequence returned by RNAiFold2T, it follows that at temperature } T_1 (resp. } T_2), \text{ each subsequence of the solution that corresponds to a node in decomposition tree } T_1 (resp. } T_2) \text{ folds into the corresponding substructure of target } S_1 (resp. } S_2). \text{ The top portion of Figure 1 illustrates the differences between EH and EHwD decomposition, and when a check is made for whether the target substructure agrees with the MFE structure of the instantiated subsequence. In the sequel, we refer to four types of elements in an EHwD:}

- Dangling position: Unpaired position at any side of a helix.
- Unpaired position: Any other unpaired position.
- Closing base pair: Outermost base pair of a helix.
- Normal base pair: Any other base pair.

1.4 Heuristics for variable and value order

In a CP algorithm, one typically specifies the order in which variables are instantiated (assigned), known as the variable ordering heuristic, as well as the order in which the values belonging to the domain of each variable are to be assigned, known as the value ordering heuristic. The variable ordering heuristic is divided into two levels: first, the order in which EHwDs are to be assigned, and second, the order in which nucleotide positions within helices are to be assigned. In this section, we also discuss restarting heuristics for the Large Neighbourhood Search (LNS) variant of RNAiFold2T.

1.4.1 Variable ordering at the helix level

In the search for thermosensors, there is often an overlap between EHwDs of structure } S_1 \text{ and those of structure } S_2—\text{this situation substantially complicates the task of finding an optimized order of exploration of the CP search space. In the leaf-to-root heuristic of RNAiFold 2.0, EHwD node } H_0 \text{ is explored before EHwD node } H' \text{ if the height } \text{ht}(H)_0 \text{ of } H_0 \text{ is less than the height } \text{ht}(H')_0 \text{ of } H', \text{ or if } \text{ht}(H)_0 = \text{ht}(H')_0 \text{ and } H_0 \text{ appears to the left of } H' \text{ in the decomposition tree for the single target structure } S. \text{ In contrast to this heuristic, RNAiFold2T implements two different approaches in order to find an adequate exploration ordering for the EHs with dangles for two target structures } S_1 \text{ and } S_2, \text{ whereby a high priority is given to solve those helices, whose sequence is determinant for other parts of the structure due to overlaps. Let } N \text{ denote the number of nodes (EHwDs) in the decomposition tree for } S_1, \text{ plus the number of nodes (EHwDs) in the decomposition tree for } S_2. \text{ Suppose that } H, H' \text{ are two distinct EHwDs belonging to } S_1 \text{ or } S_2, \text{ where the outermost base pair of } H (resp. } H') \text{ is } (i, j) \text{ (resp. } (i', j')). \text{ Define the following relations:}

- includes}(H, H') \text{ is 1 if } i < i' \text{ and } j > j', \text{ i.e. interval } [i, j] \text{ properly contains } [i', j']; \text{ otherwise includes}(H, H') \text{ is 0.}
- overlap}_1(H, H') \text{ is 1 if } [i, j] \cap [i', j'] \neq \emptyset, \text{ or equivalently } \max(i, i') \leq \min(j, j'); \text{ otherwise overlap}_1(H, H') \text{ is 0.}
- overlap}_2(H, H') \text{ is the number of positions } k \text{ in } H \text{ and } H', \text{ for which } k \text{ is base-paired in both } H \text{ and } H'.
- degree}_z(H) = \sum_{x=0}^{N} overlap}_z(H, H_i), \text{ for } z = 1, 2.
For $\alpha = 1, 2$, $\degdist(a(H, H'))$ is equal to $\deg(e_e(H) - e_e(H'))$, provided that $\deg_e(H) > \deg_e(H')$; otherwise, $\degdist(a(H, H')) = 0$.

For $\alpha = 1, 2$, $\diff((\sigma, H, H'))$ is equal to $\degdist(a(H, H'))$, provided that $\sigma(\text{label}(H)) < \sigma(\text{label}(H'))$; otherwise $\diff((\sigma, H, H')) = 0$.

The value $\text{label}(H)$ is defined in Supplementary Material, and corresponds to visitation order in breadth-first traversal of tree $T$, and $\sigma: \{0, \ldots, N - 1\} \rightarrow \{0, \ldots, N - 1\}$ is a permutation that minimizes $\sum_{j=0}^{N-1} \sum_{k=0}^{N-1} \mathbf{diff}(\sigma(H_k), H_j)$, subject to the constraint that if $H$ properly includes $H'$, then $\deg(H) > \deg(H')$. Note that the partition $\pi$ orders the EHwDs of $S_1$ and $S_2$ in order to minimize the total incremental overlap. Before the search for thermosensors begins, RNAiFold2T executes a very fast CP search to determine the optimal ordering permutation $\sigma$. Finally, by setting the index $\pi$ to either 1 or 2 in the definition of $\mathbf{diff}(\sigma, H, H')$, we obtain the first or second search heuristic. (Two additional helix ordering heuristics are explained in Supplementary Material.) An example of each helix order heuristic 1, 2 is shown in Figure 1—note that for even small structures, there are several differences in the helix traversal order when $\pi$ is 1 or 2.

1.4.2 Variable ordering at the nucleotide level

The second level of variable ordering heuristic deals with the exploration of nucleotide positions within a given EHwD structure. This second level of variable ordering can be stated as follows:

First, non-outermost base-paired positions ($x, y$) of a given EHwD are instantiated from the innermost base pair to the outermost base pair.

Second, unpaired positions in a given EHwD are grouped together in consecutive runs, and these runs are ordered from largest to smallest and then instantiated from left to right.

Third, the outermost, closing base pair of a given EHwD is instantiated.

Finally, dangling positions of a given EHwD (if any) are instantiated (note that not all EHwDs contain dangling positions).

The small example shown in Figure 2 graphically depicts the differences between constraint checks and variable ordering for both RNAiFold and RNAiFold2T. Supplementary Tables S1 and S2 describe and benchmark variable and value heuristics in RNAiFold2T.

1.4.3 Value ordering

Value ordering establishes the order in which values are assigned to variables—in our case, this means values GC, CG, AU, UA, GU, UG for base-paired positions and A, C, G, U for unpaired positions. The underlying idea for ordering domain values for variables for base-paired positions and unpaired positions is to allow the creation of thermodynamically stable helices and to take into account the nature of the overlap in overlapping positions. This requires specific value orderings for base-paired positions, depending on whether the position is a dangle, mismatch, normal or closing base pair of an EHwD for both targets $S_1, S_2$, or only one of the target structures. For each of these cases, we define different ordering heuristics, described in Supplementary Table S1.

1.4.4 LNS restart heuristics

Similarly as in the LNS variant of RNAiFold, the restart condition is a given amount of time, proportional to the length of the target structures, after which search is stopped and some variables are fixed in order to explore exhaustively a large neighborhood of the current solution. After the first restart, full exploration of the remaining space with no solution found is also a restart condition.

In RNAiFold2T, when a restart is triggered, a set of positions is selected as candidates to be fixed. The MFE structure for each EHwD of the current candidate solutions is evaluated independently. If the MFE structure of an EHwD matches with the target structure at the desired temperature, and the MFE structure of all the overlapping helices in the second target structure (at the corresponding temperature) also matches, then all the EHwD positions are included in the set of candidates. When all the EHwDs have been evaluated, candidate positions are fixed with a probability of 0.9, and the set of candidate positions is stored.

Since the order of exploration is similar in each round, it could be possible that fixing similar parts of the sequence results in an exploration of almost the same region of the search space in subsequent searches, so two mechanisms are implemented to avoid this behavior: (i) in subsequent restarts, if the candidate positions to be fixed are the same as in the previous restart, then the probability of fixing positions decreases by 0.05, if not, then the initial probability of 0.9 is restored. (ii) There is a hard restart (no nucleotide position is fixed) in the case that, after 10 restarts, the set of candidate positions remains unchanged, or if all possible solutions for the current subproblem have been explored.

In local search algorithms, there is always a trade-off between exploitation and exploration. Exploitation means focusing the search on promising regions, as reflected in our choice of probability 0.9 to remain close to currently instantiated portions of the sequence. Exploration means covering different, remote regions of the search space, as reflected in our choice to decrement the probability by 0.05 and our choice to perform a hard restart after 10 restarts.

1.5 Benchmarking

1.5.1 Benchmarking data

We retrieved the sequences of seven families of non-coding RNA thermometers from Rfam: RF00038, RF00433, RF00435, RF01766, RF01795, RF01804, RF01832. These families include both cold and heat shock RNA thermometers, taken from diverse organisms including phages, prokaryotes and eukaryotes, with sequence length ranging from 60 nt to 450 nt. The benchmarking was divided into two groups: sequences shorter than and longer than 130 nt. For each sequence, we used RNAfold (Lorenz et al., 2011) with the Turner99 energy parameters (Turner and Mathews, 2010) to determine the MFE structures at temperatures $T_1$ and $T_2$, where temperatures were chosen (essentially) according to published experimental studies for each thermometer family (Altvia et al., 1989; Chowdhury et al., 2003; Rinnenthal et al., 2011)—in particular, we increased the temperature difference $T_2 - T_1$ from the published values to ensure that RNAfold produced distinct structures at $T_1$ and $T_2$ if possible (Supplementary Material). Turner99 rather than Turner2004 energies were used, since it required less distortion to published temperatures $T_1$, $T_2$. All sequences, whose MFE structures at $T_1$ and $T_2$ were identical, were subsequently removed. See Supplementary Tables S3–S5 and Supplementary Excel files for benchmarking results, and Supplementary Table S6 (resp. Supplementary Excel file) for a list of sequences, structures, and temperatures for sequences of length less than 130 nt (resp. greater than 130 nt). The resulting benchmark set includes all 5 Lambda phage CIII thermoregulator elements (Lambda thermo), all 3 FourU thermometers, 11 of 13 repression of heat shock (ROSE) elements, 8 of 14 sequences from a second family of repression of heat shock (ROSE_2) elements, 3 of 13 thermoregulators of PrfA virulence
genes (PrfA), 4 of 6 HSP90 cis regulatory elements (HSP_CRE) and 14 of 15 cold shock protein regulator sequences (CspA).

1.5.2 Software used in benchmarking tests
SwitchDesign (SD) (Flamm et al., 2001), Frnakenstein (FRNA) (Lyngso et al., 2012), and RNAiFold2T were benchmarked on Rfam family RF01804 of Lambda phage CIII thermoregulator elements to determine the maximum number of distinct solutions over 24 h, restarting when no new solution is found within 1 h. Since neither FRNA nor SD output more than one solution, we made the following modifications of each program. The genetic algorithm Frnakenstein was run as many times as possible over 24 h (each time with a time limit of 1 h); we then output all sequences found in the most recent (internally stored) population which fold into the target structures $S_1$, $S_2$ at temperatures $T_1$, $T_2$. SD returns a single sequence which minimizes a cost function described in Flamm et al. (2001); thus we modified SD source code in order to test whether any sequence explored in the search was a solution. Sequences were checked at two different points in SD: when a new sequence is generated by a single mutation (SD update), and when a sequence is selected by minimization of the cost function (SD selected). In all cases, SwitchDesign was restarted if no new sequence was found in 1 h.

For each solution set obtained, additional solutions were generated by testing all single point mutations of any solution returned. Additionally, a reference solution set was produced by running RNAiFold2T for several days.

2 Results

2.1 Design of thermo-IRES switches
Domain 5 of wild-type FMDV IRES element contains the 46 nucleotides AUAGGUGACC GGAGGUCGGC ACCUUUCCUU UACAAUUAAU GACCCU at positions 417–462, as shown in Figure 1 of Fernandez et al. (2011), where we added AUG start codon at positions 47–49 (corresponding to IRES positions 463–465).

Using RNAiFold2T, 24,410 solutions were generated, although an additional 45,442 sequences were generated using variants of target $S_1$. Remaining curves are for Frnakenstein (light green), SwitchDesign (dark green and purple) and RNAiFold2T (red). Arrows indicate cost values for the real λ phage CIII thermoregulators from Rfam RF01804. Distribution for SD and FRNA without additional single point mutants shown in Supplementary Material. Supplementary Figures S1 and S3 show clearly that cost function values for Rfam sequences approximately equal the reference distribution mean.

**Fig. 3.** (a and b) Target structures $S_1$ at temperature $30^\circ\text{C}$ (a) and $S_2$ at temperature $42^\circ\text{C}$ (b) for domain 5 thermo-IRES element with added AUG codon (blue). IUPAC sequence constraints are determined from an alignment of 183 IRES sequences as shown in Figure 1 of Fernandez et al. (2011). Domain 5 stem-loop (positions 3–24 in red) and unpaired polypurine tract (PPT region) at positions 44–47, are both known to be essential for IRES activity (Kuhn et al., 1990). Target structure $S_1$ was designed to sequester the PPT at low temperature, thus creating a thermo-IRES which should be functional only at high temperature. (c) Ratio of normalized IRES activity at $42^\circ\text{C}$ over that at $30^\circ\text{C}$ for wild-type FMDV IRES, a negative control, and two thermosensors designed using RNAiFold2T.

**Fig. 4.** Relative frequency of the cost function optimized by SwitchDesign, for solutions returned by RNAiFold2T, SwitchDesign and Frnakenstein, given target structure $S_1$ (resp. $S_2$) at temperature $T_1$ (resp. $T_2$) for λ phage CIII thermoregulators from Rfam RF01804. This figure is a more generous representation of the data from SwitchDesign and Frnakenstein, since all single point mutant solutions have been added to the raw output.

(Supplementary Figure S1 presents histograms for the raw output of these programs.) The reference distribution for RNAiFold2T (Reference black curve), was produced by running RNAiFold2T for several days. Remaining curves are for Frnakenstein (light green), SwitchDesign (dark green and purple) and RNAiFold2T (red). Arrows indicate cost values for the real λ phage CIII thermoregulators from Rfam RF01804. Distribution for SD and FRNA without additional single point mutants shown in Supplementary Material.
• Probability $Pr(S_1, T_1)$ of active conformation at $T_2 = 42\,^\circ C$ exceeds 0.2.
• Probability $Pr(S_1, T_1)$ of inactive conformation at $T_1 = 30\,^\circ C$ exceeds 0.2.
• Probability of intended target structure at intended temperature is more than double that of unintended target, i.e. $Pr(S_1, 42)/Pr(S_1, 30) < 0.5$ and $Pr(S_2, 30)/Pr(S_1, 30) < 0.5$.

3. Retained solutions were further filtered using various measures. For instance, candidate 1 (Seq1) had the highest value of $A + B$, where $A$ is $a \cdot (b \cdot Pr(S_1, 30) + c \cdot (Pr(S_1, 30) - Pr(S_2, 30)))$ and $B$ is $d \cdot (1 - Pr(S_1, 30)) + e \cdot (b \cdot Pr(S_2, 42) + c \cdot (Pr(S_1, 42) - Pr(S_2, 42)))$, and $a = 4, b = 0.5, c = 0.5, d = 2, e = 1$. This measure was designed to select sequences where the probability of the intended target at the intended temperature is high, while probability of the unintended target is low. The measure is weighted to increase the likelihood of not having the inactive conformation at 42°C. In contrast, Candidate 2 (Seq2) is one of two sequences satisfying $Pr(S_2, 42) > 0.3$ and $P(S_2, 30) > 0.3$. See Supplementary Material for a spread sheet of measures and their values.

Seq1 and Seq2 consist of the following 46 nt: Seq1 is AAUAGGUACC GGAGGCGGACC CUUUUUC CAGAA and Seq2 is GUAGGUGACC GGAGGGCGGC ACCUUUUUUC CAGAAA.

2.2 Comparison of RNAiFold2T with other software
Here we compare the CP and LNS programs of RNAiFold2T with the adaptive walk program SwitchDesign (SD) (Flamm et al., 2001) and the genetic algorithm Frnakenstein (FRNA) (Lyngso et al., 2012). Below, we describe benchmarking results for datasets of thermosensor target structures $S_1$ resp. $S_2$ at temperatures $T_1$ resp. $T_2$, constructed as described in Section 1. All benchmarking was carried out on a Core2Duo PC (2.8 GHz; 2 Gbyte memory; CentOS 5.5).

SD, the first algorithm capable of designing thermoswitches, achieves this by optimizing the cost function given in Equation (7) of Flamm et al. (2001)—see also Equation (1) in Supplementary Material. In this context, we wanted to ascertain whether natural thermoswitches are optimized for this cost. Surprisingly, Figure 4 and Supplementary Figure S1 show that natural thermosensor sequences from RFam appear not to be optimized for the cost function used in SD. In particular, SD and FRNA return solutions having substantially lower cost values (i.e. more optimal) than those of natural thermosensors, whose cost value appears to be the mean value returned by RNAiFold2T. Therefore, our benchmarking comparison of SD, Frnakenstein and RNAiFold2T compares the number of problems solved by each algorithm within the same amount of time.

Supplementary Table S1 describes the value ordering heuristics used in RNAiFold2T; Supplementary Table S2 benchmarks RNAiFold2T with respect to different helix ordering and value heuristics, using a cutoff time of 10 min. Since the data clearly demonstrate the superiority of overlap2 helix ordering, this is taken as the default for all other benchmarks and for the web server. Supplementary Table S3 (resp. Supplementary Table S4) presents benchmarking data for LNS from RNAiFold2T and SwitchDesign and Frnakenstein, each with a cutoff time of 30 min, using RFam thermosensor target structures of length less than 130 nt (resp. greater than 130 nt)—see Section 1 for construction of target structures and temperatures. RNAiFold2T has essentially the same performance as SD and FRNA for shorter sequences, while SD performs better than other methods for longer sequences. Target structures $S_1$, $S_2$ and temperatures $T_1$, $T_2$ for this test are given in Supplementary Table S5 displays the number of solutions for a phage CII thermoswitches from Rfam family RF01804. CP from RNAiFold2T, adaptive walk SwitchDesign (Flamm et al., 2001) and genetic algorithm Frnakenstein (Lyngso et al., 2012) were run on each thermosensor for 24 h, forcing a restart if no new solution was found within 1 h. Since both SwitchDesign and Frnakenstein return only a single solution, for this test we modified each as described in Section 1, resulting in two versions of SwitchDesign and one of Frnakenstein, each of which returns two orders of magnitude less solutions than RNAiFold2T. Supplementary Table S6 lists the target structures $S_1$, $S_2$ and temperatures $T_1$, $T_2$ of RNA thermometers of length less than 130 nt used in the benchmarking tests. The structures for thermometers of length 130–447 nt are too large for display, hence are available in an Excel file in Supplementary Material.

3 Discussion
In this article, we introduce the software RNAiFold2T, capable of solving the inverse folding problem for two or more temperatures, i.e. generating one or more RNA sequences whose MFE secondary structures at temperatures $T_1$ and $T_2$ (resp. $T_1, \ldots, T_n$) are user-specified target structures $S_1$ and $S_2$ (resp. $S_1, \ldots, S_n$), or prove that none such solution exists. RNAiFold2T is unique in that it implements two different algorithms—CP and LNS. CP is an exact, non-heuristic method that uses an exhaustive yet efficient branch-and-prune process, and is the only currently available software capable of generating all solutions or determining that no solution exists (since there are possibly exponentially many solutions, a complete solution is feasible only for structures of modest size). CP differs from what one might call a ‘brute-force’ approach only in that it relies on a highly efficient branch-and-prune search engine, which propagates the effects of currently instantiated variables held within a constraint store. LNS uses a local search heuristic, complemented with local calls of CP to explore solutions of substructures of the target structures.

There exists an RNA sequence compatible with any two given secondary more than two structures (Reidys et al., 1997)—nevertheless, RNAiFold2T solves inverse folding problem for more than two temperatures. RNAiFold2T is modular software, with a clear separation between search procedure and constraint descriptions, thus permitting the future addition of sequence and structural constraints. In its current form, RNAiFold2T includes constraints for full and/or partial target structures or hybridization complexes at two temperatures; a plug-in to use RNAfold or RNAstructure for MFE structure computation; IUPAC nucleotide constraints, IUPAC amino acid constraints that require all returned RNA sequences to code specified peptides in one or more overlapping reading frames, structural compatibility and structural incompatibility constraints, etc. These constraints support the design of temperature-sensitive selenocysteine insertion (SECIS) elements, precursor microRNAs and mRNA domains that are targeted by microRNAs, etc. Since CP is not a heuristic, unlike other methods such as adaptive walk, genetic algorithm, etc., RNAiFold2T can in principle return all 2-temperature inverse folding solutions, or prove that none exist. The LNS algorithm of RNAiFold2T returns a single solution with approximately the same performance as state-of-the-art approaches SD and FRNA.
As with the synthetic hammerhead design in Dotu et al. (2015), our synthetic RNA design strategy consists of generating many solutions, which are prioritized for experimental validation by applying various computational filters. In our opinion, this strategy presents advantages over methods using SD or NUPACK, each of which returns a relatively small number of sequences that are optimized with respect to a single criterion—in the case of SD, this is the cost function (Flamm et al., 2001), and in the case of NUPACK, this is ensemble defect (Zadeh et al., 2011).

In order to ascertain the viability of our approach of not committing to a particular cost function, we used the capabilities of RNAiFold2T to find hundreds of thousands of solutions to the 2-temperature inverse folding problem for target structures from Rfam family RF01804 (λ phage CIII thermoregulators). Figure 4 and Supplementary Figure S1 show that the cost function value of (real) Rfam sequences is not close to the minimum, but rather close to the average of the distribution. Other figures can be found in Supplementary Material, where we investigated a variant of the cost function defined using ensemble defect. So, although SD benchmarking results in Supplementary Material indicate that cost function minimization is a good strategy to find sequences whose MFE structures at temperatures $T_1$ resp. $T_2$ are the target structures $S_1$ resp. $S_2$, it appears that naturally occurring RNA thermoswitches are not optimized for the SD cost function. This observation may be important for the future design of functional synthetic thermoregulators.

In designing thermo-IRES elements, we solved the 2-temperature inverse folding problem depicted in Figure 3, where the AUG start codon was appended at the 3’ end of the 46 IUPAC constraint mask UAGGNGACC GNAGNCGGC NCUUYYYYY YRNNNN NNNN NNNN. This was done since we assumed that the AUG start codon was located at position 463, as it occurs in the viral RNA. However, experimental validation was performed by using a construct containing the 35 nt spacer GAGCUGAGC UUGGCAAUUC GGUACUGUUG GUAAA at the 3’ end of the designed 46 nt sequences, followed by the luciferase AUG start codon. It is possible that the secondary structure of the spacer might have rendered the polypyrimidine tract less accessible, thus explaining the low efficiency of thermo-IRES constructs Seq1 and Seq2. Another issue is that IRES elements are complex molecules, both in sequence and structure, which respond to more host factors than previously reported RNA thermometers (Lozano and Martinez-Salas, 2015). Secondary structure predictions could differ from the physical structure due to unmodeled protein-RNA interactions, possibly unreliable free energy parameters at temperatures different than 37°C, and due to variations in structure prediction software as shown in Figure 5. Panels (a) resp. (b) of Figure 5 show that the polypyrimidine tract (PPT) is unpaired in the secondary structure of domain 5 of wild-type IRES at 37°C (hence consistent with experimental data), when determined by RNAfold (without SHAPE) resp. RNAsc (with SHAPE) (Zarringhalam et al., 2012), while panels (c) and (d) of Figure 5 show the PPT is paired in the structure determined by RNAstructure, both with and without SHAPE (Deigan et al., 2009) (hence inconsistent with experimental data). Due to this variation in MFE structure prediction, it may be advisable in future synthetic RNA design projects to run RNAiFold2T using plug-ins for both RNAfold and RNAstructure, and to select sequences which have the same desired target structures as predicted by both algorithms. Another issue is that for many RNA thermometers, the MFE structures at low temperature $T_1$ and high temperature $T_2$ are almost identical, where $T_1$, $T_2$ are the temperatures for which a conformational change is reported in the literature. For instance, the MFE structures for the ROSE element CP000009.1/1450710-1450627 at 0°C and 60°C are nearly identical. This could be an important issue for certain software (Churkin et al., 2014; Chursov et al., 2013) that predict RNA thermometers, but is of less importance in the synthetic design of thermometers, where it is possible to exaggerate the temperature difference $T_2 - T_1$. Perhaps future experimental work will provide more reliable energy parameters at temperatures different than 37°C, an issue that affects both RNA and DNA melting temperature predictions (Rouzina and Bloomfield, 1999).

### 4 Conclusions

We present the software RNAiFold2T for the multi-temperature inverse folding problem, used to design functional thermoswitches. The CP variant of RNAiFold2T returns two orders of magnitude more solutions than other software, while the LNS variant, which returns a single solution, exhibits comparable performance with that of existent methods. The software design of RNAiFold2T currently supports a much greater variety of user-defined structural and sequence constraints than other methods, and moreover can be extended to support future constraints.

Naturally occurring RNA thermometers in heat-shock and virulence genes, as well as all previously known instances of rationally designed thermometers control translation initiation by sequestering the Shine-Dalgarno ribosomal binding sequence at low temperatures (Flamm et al., 2001).
temperatures, whereby this sequence becomes accessible at high temperatures due to the melting of a hairpin. In contrast, we have used RNAiFold2T to design a temperature-regulated internal ribosomal entry site (IRES) element by ensuring the presence at high temperatures of the domain 5 stem-loop and downstream single-stranded pyrimidine (Py) tract, both located upstream of the functional initiation codon and both known to be important for IRES functionality (Lozano and Martinez-Salas, 2015). At low temperatures, our thermo-IRES element is designed to adopt a conformation that down-regulates protein product by disrupting both the domain 5 stem-loop and sequestering the Py tract. We showed that our rationally designed thermo-IRES elements are functional, where the cap-independent translational efficiency is approximately 50% higher at 42°C than at 30°C; however, since the focus of this article is primarily to describe a new method, we have not taken steps to improve efficiency using error-prone mutagenesis and selection.

**Funding**

Research of the Clote Lab was supported by National Science Foundation grant [DBI-1262439]. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the National Science Foundation. Research of the Martinez-Salas Lab was supported by the Spanish Ministry of Economy and Competitiveness (MINECO) [CSD2009-00080, BFU2011-25437, BFU2014-54564] and by an Institutional Grant from Fundación Ramón Areces.

**References**


