Roughness-dependent tribology effects on discontinuous shear thickening

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Surface roughness affects many properties of colloids, from depletion and capillary interactions to their dispersibility and use as emulsion stabilizers. It also impacts particle–particle frictional contacts, which have recently emerged as being responsible for the discontinuous shear thickening (DST) of dense suspensions. Tribological properties of these contacts have been rarely experimentally accessed, especially for nonspherical particles. Here, we systematically tackle the effect of nanoscale surface roughness by producing a library of all-silica, raspberry-like colloids and linking their rheology to their tribology. Rougher surfaces lead to a significant anticipation of DST onset, in terms of both shear rate and solid loading. Strikingly, they also eliminate continuous thickening. DST is here due to the interlocking of asperities, which we have identified as “stick–slip” frictional contacts by measuring the sliding of the same particles via lateral force microscopy (LFM). Direct measurements of particle–particle friction therefore highlight the value of an engineering-tribology approach to tuning the thickening of suspensions.

Significance

Shear thickening is a ubiquitous rheological phenomenon whereby dense suspensions of particles in a fluid exhibit a viscosity increase at high shear, which can turn into a viscosity divergence [discontinuous shear thickening (DST)]. Although macroscopically well characterized, the microscopic origin of DST is still debated, especially in connection to particle surface properties, e.g., roughness and friction. We elucidate here the mechanisms underpinning DST by carrying out nanotribological measurements of the interparticle contacts of model rough colloids. We demonstrate that rough particles exhibit DST over a broader range of shear rates and for volume fractions much lower than for smooth colloids, due to interlocking of surface asperities, showing that taking an engineering-tribology approach is a powerful way to tune DST.


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shown in Fig. 1H. We synthesize a library of raspberry-like silica particles with $0 < h/d < 0.53$, covering a broad roughness range from the smooth cores to the roughest raspberry. Hereon, the smooth cores are named “SM” and the raspberry-like particles “RB, $h/d$”, where $h/d$ is the value of the dimensionless roughness parameter for each batch. (See SI Materials and Methods for further details.)

We first quantify the role of surface roughness on the maximum packing fraction $\phi_m$ of the particles in a sedimentation/compressive rheology test. This quantity represents the limit at which the suspension can be processed, i.e., the volume fraction for which the suspension jams at vanishingly small rates. Our previous work showed that $\phi_m$ is directly correlated to the interparticle friction coefficient (23). As opposed to the case of non-Brownian particles, $\phi_m$ can slowly evolve with time due to the combined effects of thermal fluctuations and sedimentation (more details in SI Materials and Methods and Fig. S1). $\phi_m$ can be estimated by measuring the height of the sediment starting from a dilute suspension of known solid loading (Fig. 2A). Fig. 2B shows that the sediment height increases with the initial volume fraction, as expected. Rougher colloids present $\phi_m$ values that are clearly lower than those of smooth colloids (Fig. 2C). This indicates that rougher particles, i.e., with higher $h/d$ values, jam earlier during sedimentation and, as a result, the sediment is looser. Remarkably, particles with $h/d = 0.53$ jam under centrifugation for solid loadings as low as 44.5%, indicating that roughness has a dramatic impact on DST and can be very effectively used to engineer the suspension’s rheological response.

In fact, smooth colloids (SM, Fig. 2D) start to display CST for $\phi > 51\%$ and exhibit DST behavior only at $\phi = 58\%$, which is very close to their measured $\phi_m$ of 59.2%. The first normal stress difference $N_1$ remains negative between 48% and 58% during CST, while it switches sign at the onset of DST, which is characteristic of frictional dilatant flows. Rough colloids, on the other hand, show a qualitatively different behavior. Raspberry-like particles with $h/d = 0.53$ do not show any appreciable CST, but immediately discontinuously thicken, even for values of $\phi$ significantly lower than their $\phi_m$ (Fig. 2E), and the onset of DST shifts to lower $\phi$ with increasing $h/d$. It is also worth noting that the critical rate varies over almost two decades, compared with a much narrower window for the smooth colloids. Correspondingly, the viscosity increase is always associated with a positive $N_1$, indicating that DST in our experiments is always associated with dilation-inducing interparticle contacts, as opposed to cases dominated by hydrodynamics, where large viscosity jumps occur for negative $N_1$ (29). Moreover, Fig. 2F shows that, at the same solid loading of $\phi = 48\%$, rough colloids with different roughnesses exhibit DST, while smooth colloids do not thicken at all. The critical DST shear rate depends on the distance from $\phi_m$: The closer $\phi$ is to $\phi_m$, the lower the observed critical shear rate. Interestingly, an analogous trend of the suspensions’ nonlinear response with volume fraction and surface roughness is observed in the ball-impact tests displayed in Movies S1–S8 (SI Materials and Methods). Even though the deformation here is more complex (30) than in the pure shear experiments, the link between shear rheology and impact absorption has already been exploited in applications (4).

To account for these rheological observations, we turn to studying microscopic particle-to-particle contacts. These measurements are carried out by means of lateral force microscopy (LFM), where smooth and rough colloids are attached onto tipless cantilevers (Fig. S3) and scanned over planar substrates of varying roughness (roughness gradients), as shown in Fig. 3A and B (see SI Materials and Methods for further details). The substrates are produced by a process analogous to the synthesis...
of the rough colloids, to provide representative, realistic countersurfaces (SI Materials and Methods and Fig. S2). The LFM results from sliding an RB,0.53 probe over a roughness gradient with 22-nm-high asperities are shown in Fig. 3C. (See Figs. S4–S7 for the friction results of all other particles.) Starting from the smooth end of the sample (Fig. 3C, rightmost curve, magenta), we observe a very narrow friction loop, i.e., a small difference in the lateral force signals between trace and retrace of the same scan on the substrate, indicative of a low friction coefficient. As soon as the area density of asperities increases, distinctive spikes arise in the friction-loop scans (Fig. 3C, cyan curve). These are typical of stick–slip frictional behavior. During scanning, when the probe meets an asperity, the lateral force increases steeply as the probe becomes locally stuck and then rapidly slides as the asperity is overcome. The frequency of the stick–slip events increases with increasing roughness (Fig. 3C, from right to left), which corresponds to higher dissipation during scanning and hence to an increase in the friction coefficient \( \mu \) (Fig. 3D). We remark here that we measure “effective” friction coefficients, which already take into account the geometry of the contact, with interlocking asperities. The Amontons-type relation, \( F_{\text{friction}} = \mu \cdot F_{\text{load}} \), holds very well in our experiments, as shown in Fig. 3D. The nature of the frictional interactions between rough surfaces also motivates our choice to describe surface roughness by the parameter \( h/d \), since the stick–slip events are determined by the asperities’ amplitude and periodicity (31), which are also the parameters we tune in the fabrication of our colloids.

Interestingly, smooth and rough probes sliding on surfaces with increasing \( h/d \) roughness give rise to different frictional
Friction measurements on model rough substrates. (A) Schematics of a smooth probe on a rough sample and SEM image of a smooth colloidal probe. (Scale bar, 500 nm.) (B) Schematics of a rough probe on a rough sample and SEM image of an RB,0.53 colloidal probe. (Scale bar, 500 nm.) (C, Top) RB,0.53 probe scanning at different locations on a 22-nm rough gradient substrate. (C, Bottom) Friction loops at 60 nN applied load for various $h/d$ roughness on the substrate ($h/d = 0.53$, black; $h/d = 0.39$, red; $h/d = 0.35$, green; $h/d = 0.29$, blue; $h/d = 0.23$, cyan; $h/d \approx 0$, magenta). (Scale bar, 200 nm.) (D) Determination of $\mu$ from the measured friction forces as a function of applied load using the relation $F_{\text{friction}} = \mu \cdot F_{\text{load}}$. (E) $\mu$ vs. $h/d$ for a smooth probe (blue) and rough probes (red) on surfaces with various asperity size [12 nm (●) for RB,0.45, 22 nm (■) for RB,0.53, 39 nm (♦) for RB,0.36, and 39 nm and 12 nm (▲) for RB,0.31 and smooth and (▼) for RB,0.25). (E, Top Inset) Schematics of a smooth probe on a rough sample. (E, Bottom Inset) Schematics of a rough probe on a rough sample. (F) Correlation between $\mu$ and normalized packing fraction ($\phi_{\text{RCP}} = 0.64$). (F, Insets) Schematics of smooth particles sliding (Right) and rough particles interlocking (Left) under shear.

Generally, $\mu$ increases with surface roughness, but in a low-roughness regime ($h/d < 0.3$), there are fewer asperities on the substrate and $\mu$ is mainly determined by the contact area of the two sliding surfaces rather than by stick–slip events. Rough probes contact the substrate via the asperities on their surfaces, resulting in smaller contact area and hence lower $\mu$ compared with smooth probes. In particular, the values of friction coefficients measured between smooth silica probes and silica substrates are in agreement with literature values measured under similar conditions (32). Conversely, in a high-roughness regime ($h/d > 0.3$), the density of asperities on the surface increases, so that stick–slip events are the main contribution to friction forces. The asperities on raspberry-like particles interlock with the asperities on the substrates, leading to higher $\mu$ values than those measured for smooth particles. Fig. 3E ultimately shows that there is a direct correlation between surface roughness and friction coefficient, which uniquely depends on $h/d$ of the two surfaces.

The unique dependence of both $\mu$ and $\phi_m$ on $h/d$ makes it possible to obtain a direct relation between the first two
quantities, linking microscopic tribological properties with macroscopic rheological properties, as shown in Fig. 3F. By plotting the friction coefficients of our smooth and rough particles against surfaces with the same \( h/d \) vs. a normalized maximum packing fraction \( \phi_{\text{RCP}} = \phi_{\text{RCP}} / \phi_{\text{m}} \), where \( \phi_{\text{RCP}} = 0.64 \) is the random close packing of monodisperse frictionless spheres, we see that the higher the effective interparticle friction coefficient, the lower the maximum packing fraction at which the material can be processed before DST occurs at vanishingly small rates. Moreover, the nanotribological measurements have also shed light on the nature of the qualitative difference in the ST behavior between smooth and rough particles. For the latter, as soon as a hydrodynamic lubrication film breaks, asperities interlock, giving rise to the formation of force chains and dilatant (\( N_1 > 0 \)) DST, while smooth particles experience standard sliding friction. These observations link the details of the interparticle contacts with the global rheology, in which the interlocking of many particles leads to the viscosity increase.

Finally, this correlation allows us to engineer the macroscopic rheological response, i.e., the \( \phi_{\text{m}} \) of the suspension, by changing its nanoscopic tribological properties, i.e., the \( \mu \) between the colloidal particles. To examine this concept, we perform the sedimentation experiments on mixed colloid suspensions obtained by introducing increasing fractions of smooth particles into suspensions of rough colloids (Fig. 4). Remarkably, by replacing as little as 3.3 vol\% of the total particle number with smooth particles, \( \phi_{\text{m}} \) increases by more than 6% and the onset rate for DST at \( \phi = 0.44 \) increases by almost two decades. Increasing the percentage of smooth colloids further, \( \phi_{\text{m}} \) of the mixture tends toward the \( \phi_{\text{m}} \) of the suspension of smooth colloids, but the biggest effect is seen within the first 10%. This strong effect is due to the fact that smooth particles act like lubricants in the suspension by preventing strong interlocking between rough particles. The formation of a stress-bearing network is delayed or reduced, leading to denser packing before DST (note that the mixtures still exhibit DST and positive \( N_1 \)).

In conclusion, our results clearly confirm that there exists a strong link between the tribology of interparticle contacts and the rheology of DST suspensions. The frictional properties greatly depend on the contact geometry, and surface roughness has emerged as an essential design parameter for the thickening response. We have, for instance, shown that one can increase the solid loading and delay undesired shear thickening by introducing a small amount of particles displaying lower friction into the system, which could be of interest for slurry processing, for example. Conversely, increasing surface roughness enables a great reduction of the volume fraction, while retaining very strong thickening but having lower viscosities in the unthickened region of the flow curve, which could be of interest in fluid materials for vibration or impact absorption. As the importance of tribology in thickening fluids is increasingly becoming more widely accepted, we expect many exciting opportunities for nanoscale surface design.

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